

Staircase global warming and its deconvolution

The following graphs all use the data obtained by the National Oceanographic and Atmospheric Administration (NOAA) TIROS-N satellite, interpreted by [Dr. Roy Spencer](#) and [Dr. John Christy](#), both at Global Hydrology and Climate Center of the same University.

Records start from december,1978 and are regularly updated. They refer to four layers of the planet's atmosphere:

1. lower troposphere
2. middle troposphere
3. tropopause
4. lower stratosphere

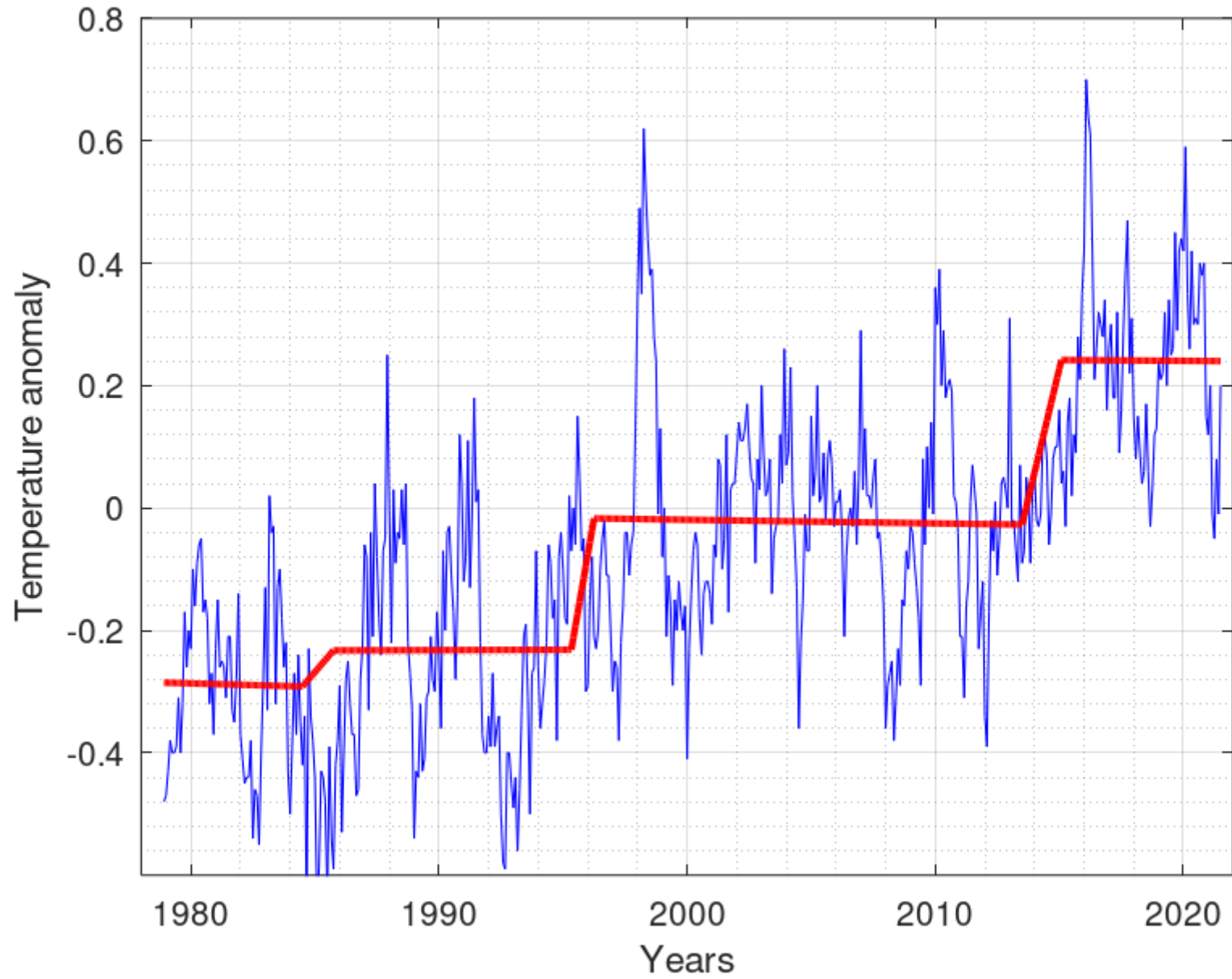
For each of the four regions of the atmosphere 24 regions of the globe are examined, namely :

3 = Globe	4 = Land	5 = Ocean	whole globe 90S-90N
6 = Globe	7 = Land	8 = Ocean	northern hemisphere 0-90N
9 = Globe	10 = Land	11 = Ocean	southern hemisphere 90S-0
12 = Globe	13 = Land	14 = Ocean	tropics 20S-20N
15 = Globe	16 = Land	17 = Ocean	northern extention 20N-90N
18 = Globe	19 = Land	20 = Ocean	southern extention 20N-90N
21 = Globe	22 = Land	23 = Ocean	north pole 60N-90N
24 = Globe	25 = Land	26 = Ocean	south pole 90S-60N

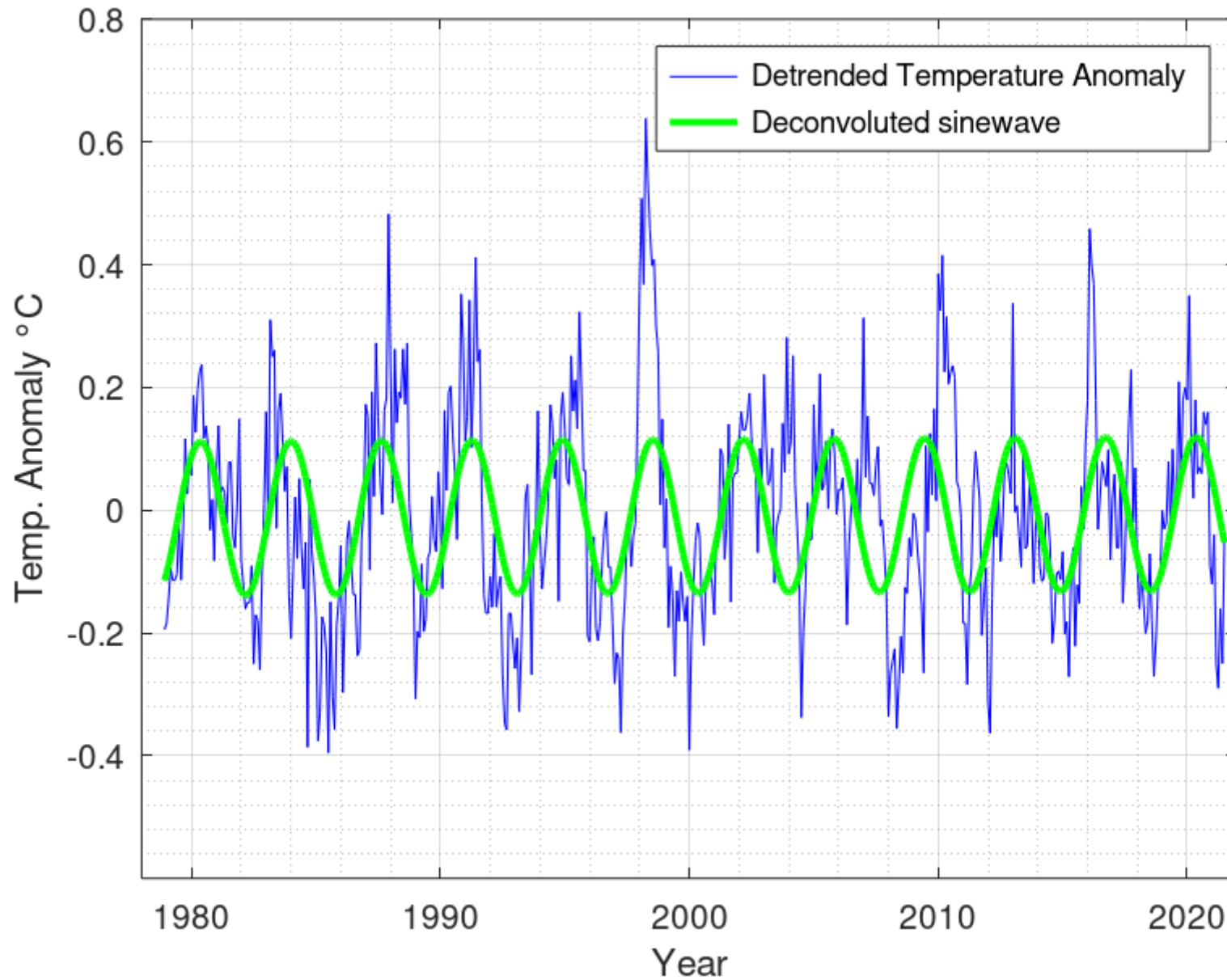
(numbers refer to the columns in the matrix)

The combination of the 4 layers with the 24 regions gives a total of $24 \times 4 = 96$ possible graphs. Here only the global data for the lower troposphere are examined, but the user can select other ragions by assigning the variable 'choice'

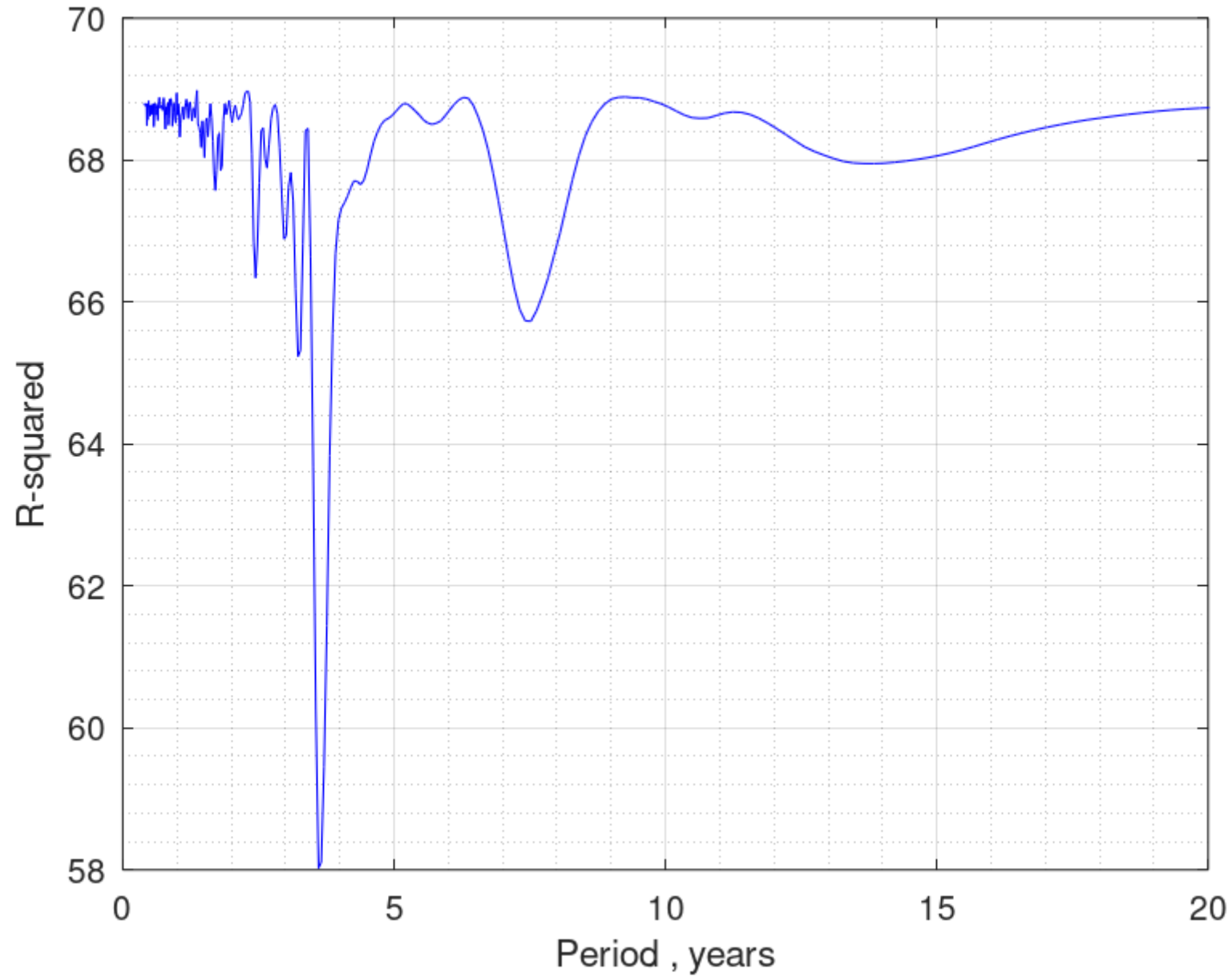
UAH Lower Troposphere - Global (updated July, 2021)



UAH Lower Troposphere - Global (updated July,2021) Period = 3.637



UAH Lower Troposphere - Global (updated July,2021)



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--->Data can be downloaded directly from UAH by this octave statement
f = urlwrite('http://vortex.nsstc.uah.edu/data/msu/v6.0/tlt/uahncdc_lt_6.0.txt','uah.txt')
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```
clear all;clc;format short;format compact;
global Ud yd xd x;
function ydRes = best(p) % ----- minimizer
    global Ud yd xd x;
    Ud(:,3) = sin(2*pi/p*x); % sin
    Ud(:,4) = cos(2*pi/p*x); % cos
    G = inv(Ud.' * Ud);
    xd(:,1) = G*Ud.'*yd;
    ydR = yd - Ud*xd(:,1); % residuals
    ydRes = sum(abs(ydR)); % sum of residuals
endfunction % ----- end of minimizer
%f = urlwrite('http://vortex.nsstc.uah.edu/data/msu/v6.0/tlt/uahncdc_lt_6.0.txt','uah.txt')
S = fileread('uahncdc_lt_6.0.txt');tit='UAH Lower Troposphere - Global (updated July,2021)'
a1 = index(S,'1978');
a2 = rindex(S,'Year Mo') - 2;
M = S(a1:a2);
X = str2num(M);
x = X(':',1) + (X(':',2)-1)./12; % date in decima year
% Average satellite of the lower troposphere refers to ...
% 3 = Globe, 4 = Land, 5 = Ocean (whole globe 90S-90N)
% 6 = Globe, 7 = Land, 8 = Ocean (northern hemisphere 0-90N)
% 9 = Globe, 10 = Land, 11 = Ocean (southern hemisphere 90S-0)
% 12 = Globe, 13 = Land, 14 = Ocean (tropics 20S-20N)
% 15 = Globe, 16 = Land, 17 = Ocean (northern extention 20N-90N)
% 18 = Globe, 19 = Land, 20 = Ocean (southern extention 20N-90N)
% 21 = Globe, 22 = Land, 23 = Ocean (north pole 60N-90N)
% 24 = Globe, 25 = Land, 26 = Ocean (south pole 90S-60N)
choice = 3;
ydT = X(':',3); % 3 = Globe can be modified

% -----
a1 = index(S,'1978 12') - 2;
a2 = index(S,'1984 8') - 2;
M = S(a1:a2);
X0 = str2num(M);xYear0 = X0(':',1) + (X0(':',2)-1)./12;
yd0 = X0(':',choice);a2 = a2/171 - 1;a1 = 1;

a3 = index(S,'1985 10') - 2;
a4 = index(S,'1995 6') - 2;
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M = S(a3:a4);a3 = a3/171;a4 = a4/171 - 1;
X1 = str2num(M);xYear1 = X1(':',1) + (X1(':',2)-1)./12;
yd1 = X1(':',choice);

a5 = index(S,'1996 4') - 2;
a6 = index(S,'2013 8') - 2;
M = S(a5:a6);a5 = a5/171;a6 = a6/171 - 1;
X2 = str2num(M);xYear2 = X2(':',1) + (X2(':',2)-1)./12; %january = 0.5
yd2 = X2(':',choice);

a7 = index(S,'2015 2') - 2;
a8 = rindex(S,'Year Mo') - 2;
M = S(a7:a8);a7 = a7/171;a8 = a8/171 - 1;
X3 = str2num(M);xYear3 = X3(':',1) + (X3(':',2)-1)./12;
yd3 = X3(':',choice);

p = polyfit(xYear0,yd0,1);y0 = polyval(p,xYear0);yNew(a1:a2) = y0;
p = polyfit(xYear1,yd1,1);y1 = polyval(p,xYear1);yNew(a3:a4) = y1;yNew(a2:a3) = linspace(y0(end),y1(1),(a3-a2+1));
p = polyfit(xYear2,yd2,1);y2 = polyval(p,xYear2);yNew(a5:a6) = y2;yNew(a4:a5) = linspace(y1(end),y2(1),(a5-a4+1));
p = polyfit(xYear3,yd3,1);y3 = polyval(p,xYear3);yNew(a7:a8) = y3;yNew(a6:a7) = linspace(y2(end),y3(1),(a7-a6+1));
yNew = yNew'; % yNew is transformed into column vector
yd = ydT - yNew;

nTot = length(yd);
Ud = zeros(nTot,4);
Ud(1:nTot,1) = 1; % constant plateau
Ud(1:nTot,2) = linspace(-1,1,nTot); % linear trend (orthogonal)
n = linspace(1,nTot,nTot);
xd = zeros(4,1);
k = 0;
for i = logspace(-0.4,1.4,300);
    ++k;
    xL(k) = i;
    pL(k) = best(i);
endfor
plot(x,ydT,'b',x,yNew,'r','LineWidth',2);
xlabel('Years');ylabel('Temperature anomaly');title(tit);grid on;
grid minor on;axis([1978,2022,-0.6,0.8]);hold on;
figure;
plot(xL,pL,'b');grid on;grid minor on;hold on;
xlabel('Period , years');ylabel('R-squared');title(tit);axis([0,20]);
figure;
%-----

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pMin = fminbnd(@best,3,5); % 1st call to the minimizer
x2 = best(pMin);pMin      % once found , pMin is given again to the best() function
ySin = Ud*xd(:,1); % y3 is the first SINEWAVE
disp(xd);
a = xd(3);b = xd(4);r = sqrt(a^2 + b^2);q = asin(b/r);      %delay for sinewave
plot (x,yd,'b',x,ySin,'g','LineWidth',2);grid on;
grid minor on;axis([1978,2022,-0.6,0.8]);hold on;
xlabel('Year');ylabel('Temp. Anomaly °C');
title([tit,' Period = ',num2str(pMin)]);
legend('Detrended Temperature Anomaly','Deconvoluted sinewave')
hold on;
```